***Greedy Algorithm:***

***Background:***

Solving the Best Optimization problem needs a series of steps, and in each step we can have multi - choices. For many Optimization problem, using Dynamic Programming Problem seems to be a storm in a teacup, we can use one more effective and more high efficient method.

***Definition - Greedy Algorithm:***

In each step, Greedy Algorithm choose the Best Solution in each step, which is to say, it always help choose Locality Best Solution in each step and hopes this kind of selection can help choose the Best Solution.

*Greedy Algorithm can not ensure to get the Best Solution, it does help many problems get the Best Solution.*

*Greedy Algorithm is a kind of Strong Algorithm Design Method which can be used to solve many problems including Minimum-Spanning-Tree Algorithm, Dijkstra Algorithm to solve the single shortest route and Chvatal Greedy Heuristic Method.*

***Activity Selection Problem:***

***Description:***

Multi-activities compete for shared resources, and the aim is to select one Biggest Compatible Activity Collection.

Assume there has only *one Activity Collection S = {a1, a2, a3, ..., an}*, and these activities share the same resource, however this kind of resource can only be used for sometime and only for one activity. *For activity ai, it has start time si and end time fi, here 0 <= si < fi < infinite.*

If it is selected, then the task ai would happen during the time period [ si, fi ). *If two activities ai and aj satisfy [ si, fi ) and [ sj, fj ) and both of which are not overlapped, then they are called compatible, which is to say, if si >= fj or sj >= fi, then ai and aj are compatible.* In the Activity Selection Problem, then we hope to choose the Biggest Compatible Activity Collection. *Assume that the activity has been sorted according to its Increasing Sequence:*

*f1 <= f2 <= f3 <= ... <= fn-1 <= fn*

*Here, that the activity has been sorted means the started time and finished time of the activity has been sorted according to its finished time.*

***Example:***

***Activity Collection***

|  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| i | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 |
| si | 1 | 3 | 0 | 5 | 3 | 5 | 6 | 8 | 8 | 2 | 12 |
| fi | 4 | 5 | 6 | 7 | 9 | 9 | 10 | 11 | 12 | 14 | 16 |

For this instance, sub - collection {a2, a9, a11} consists of different activities, but it is not the biggest collection, since the sub - collection {a1, a4, a8, a11} is bigger. Actually the sub - collection {a1, a4, a8, a11} is the bigger compatible one, and another bigger one is {a2, a4, a9, a11}.

***Solution:***

Normally, we try to divide the problem into two Sub - Question by using Dynamic Programming, and then combine two Best Solutions into one Best Solution of two Sub - Question. When make sure to use which problem to the Best Solution, then we need to take several questions into consideration.

*Greedy Algorithm needs us to take one selection into consideration (Greedy Selection), when makes Greedy Choice, one of the sub-question must be empty, therefore leave one non-empty sub-question.*

***Best Sub-Structure in Activity Selection Problem***

Assume that Sij presents that start after the end of activity ai, and end before the start of activity aj. Assume we hope to get one Biggest Compatible Activity Sub - Collection of Sij, and in further step, we assume that Aij is such Sub - Collection, including the activity aij. The Best Solution includes activity ak, then we get two separate Sub - Problem, find out the Biggest Compatible Activity Sub - Collection of Sik, and find out the Biggest Compatible Activity Sub - Collection of Skj. *(The Sik means these activities start after the end of activity ai and end before the start of activity ak. The Skj means these activities start after the end of activity ak and end before the start of activity aj.)*

Make *Aik = Aij intersection Sik, Akj = Aij intersection Sjk*, then Aik would include the activities end before the start of ak, Akj would include the activities start after the end of ak. Therefore, we have *Aij = Aik intersection { ak } intersection Akj*, and *among Sij, the Biggest Compatible Sub - Collection has | Aij | = | Aik | + | Akj | + 1 activities.*

*( By using the cut and paste method to verify that the Best Solution Aij contain the Best Solution of two Sub - Problem Sik and Skj.)*